



(Final Report)
SATELLITE TO AIRCRAFT MULTIPATH
SIGNALS OVER THE OCEAN

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ABSTRACT

A satellite-to-aircraft communication link over the ocean may include a specularly reflected signal and a diffusely scattered signal, as well as the direct path transmission. This report provides a computer program for estimating two statistical properties of the diffuse signal, namely the Doppler spectrum and the delay spectrum. A convenient representation of the total signal is also provided. Examples of the Doppler and delay spectra for a number of representative link geometries are given to illustrate the features of the diffuse signal.

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I. INTRODUCTION

One of the design limitations[1] in the development of communication links between satellites and aircraft is the presence of a secondary signal reflected from the surface of the earth. It is the purpose of this report to provide a convenient method for estimating the statistical properties of this multipath signal[2,3], particularly the power spectrum and delay spectrum, for ocean surfaces. Because the scattering properties of the sea are rather complex, it is not possible to obtain closed form expressions for these statistics. Instead a computer program, and its output for a number of representative link geometries, have been provided. These results should provide an insight into the characteristics of the multipath signal. In addition, they may be used to construct a representation of the total signal which should be adequate for most detector design studies.

The heart of the report is the computer program in Appendix I. Although conventional designations for range, angle, frequency etc. are used in the body of the report, a number of the more important identifications between report variables and the corresponding program names are provided. The latter are given in capital letters enclosed in parentheses; for example the distance R_{dir} from aircraft to satellite is called (REF) in the program.

II. THE MULTIPATH MODEL

Before giving the details for estimating the statistical properties of the multipath signal, it will be useful to describe the overall geometry of the link. This will permit an understanding of the mechanisms which produce the total receiver signal, without having to consider such extraneous factors as antenna patterns and polarizations. The basic problem in modelling the link is to estimate the relative amplitudes,

statistics, and signal distortions in the three components of the total signal transmitted from the satellite to a moving receiver.

The first component (see Fig. 1) is the direct transmission from transmitter to receiver. If a voltage reference level V_0 is chosen such that the far field radiated by the transmitter has an electric field strength V_0/R at distance R from the transmitter (i.e., the transmitter power, gain etc. are subsumed in V_0) then the receiver voltage due to the direct component will be, at time t

$$(1) \quad V_{\text{dir}}(t) = V_0(t - R_{\text{dir}}/c) h_d/R_{\text{dir}}(t)$$

where c = velocity of electromagnetic waves

$R_{\text{dir}} = TP$ = distance from transmitter to receiver

and where h_d (the effective height of the receiving antenna) accounts for the receiver properties, including pattern and polarization, in the direction of the transmitter. The distortion of the signal (the Doppler shift for a cw signal) is accounted for by the change of R_{dir} with time

$$(2) \quad R_{\text{dir}}(t) = R_{\text{dir}}(0) + (\vec{v} \cdot \vec{n}_d)t$$

where \vec{v} is the constant aircraft velocity and \vec{n}_d is a unit vector along TP.

The second component is that reflected from the surface (as if the sea were a smooth sphere) at the specular point 0. This component is given by

$$(3) \quad V_{\text{spec}}(t) = V_0(t - R_{\text{spec}}/c) \rho e^{-(kh \cos \theta_i)^2} h_{\text{sp}}/R_{\text{spec}}(t)$$

where

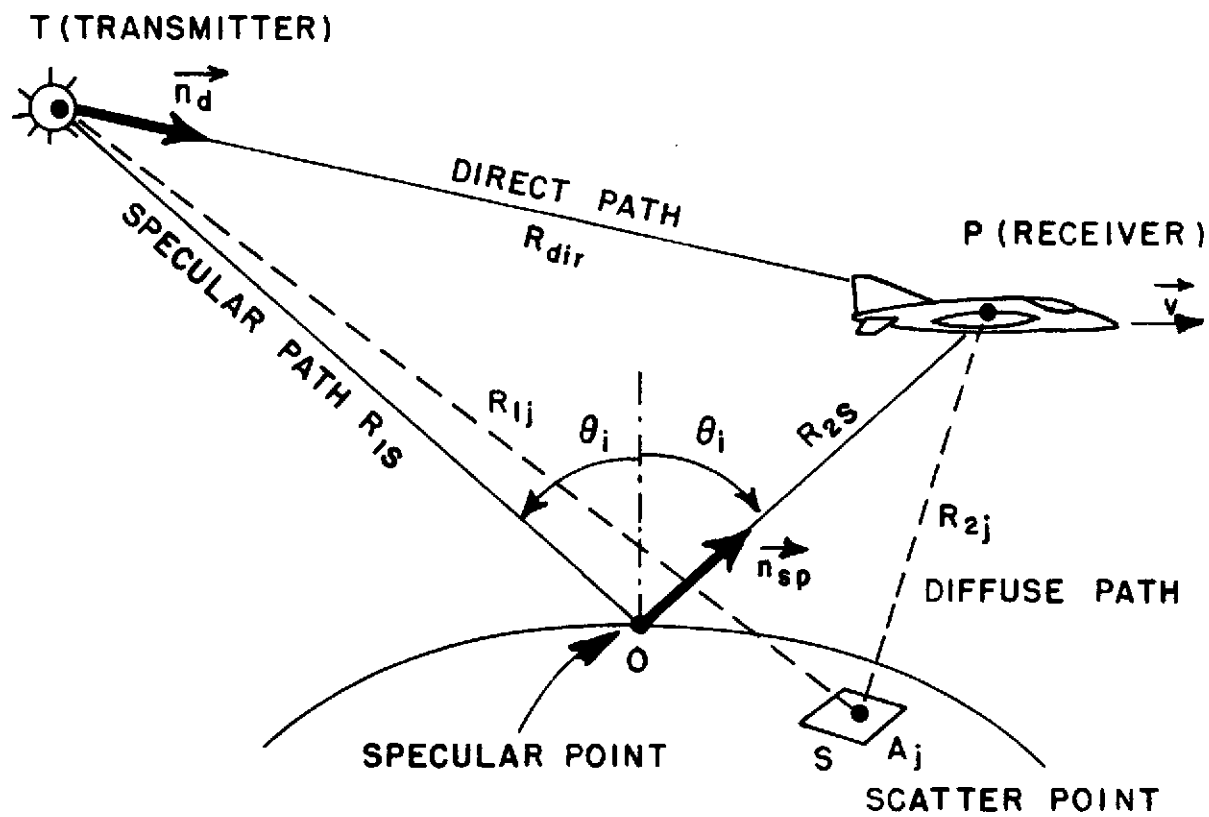


Fig. 1. Multipath links over the ocean.

$$\begin{aligned}
R_{\text{spec}} &= TO + OP \\
&= R_{1s} + R_{2s} \\
&= \text{distance along specular path} \\
\rho &= \text{voltage reflection coefficient at surface} \\
k &= 2\pi/\lambda \text{ where } \lambda \text{ is electromagnetic wavelength} \\
h &= \text{root mean square height of ocean surface} \\
\theta_i &= \text{angle of incidence at the specular point} \\
h_{\text{sp}} &= \text{antenna effective height.}
\end{aligned}$$

The exponential factor (the "Rayleigh roughness factor") accounts for the fact that since the sea surface is not smooth, some of the energy is scattered out of the specular signal. The distortion of the specular signal is also produced by the change in R_{spec} with time. If the satellite is much further from the surface than the aircraft,

$$\begin{aligned}
(4) \quad R_{\text{spec}}(t) &\approx R_{\text{spec}}(0) + (\vec{v} \cdot \vec{n}_{\text{sp}})t \\
\vec{n}_{\text{sp}} &= \text{unit vector from O to P.}
\end{aligned}$$

Clearly the direct and specular terms are coherent, albeit with differing delays or doppler shifts, so their sum $V_{\text{dir}}(t) + V_{\text{spec}}(t)$ will fluctuate (exhibit "interference", or "height gain effect") with time[3].

Finally, the diffuse or "multipath" component is a superposition of reflected fields from suitably oriented "glint points" on facets on the surface. If the location (which determines the delay) and the curvature (which determines the amplitude) of each properly oriented facet were known, one could construct the diffuse signal by superposition of the reflections from each facet. The actual sea surface is random, however, so that one must in practice be content with a representation of the diffuse signal based on certain statistical properties of the ocean surface. The simplest such surface is found by dividing up the mean surface into convenient areas A_j (see Fig. 1) and associating with each area a reflected signal whose time delay is determined by the center point, and whose

amplitude is determined by the average scattering cross-section of the area. Thus the diffuse component can be represented by

$$(5) \quad V_{\text{diff}}(t) = \sum_j \frac{V_o(t - (R_{1j} + R_{2j})/c)}{R_{1j} R_{2j}} \sqrt{\frac{\sigma_{oj} A_j}{4\pi}} h_j$$

where
 R_{1j} = TS distance from T to scatterer
 R_{2j} = SP distance from P to scatterer
 h_j = receiver effective height for j-th direction
 σ_{oj} = average cross-section per unit area[4] of j-th sub-area.

For any given choice of sub-areas, each individual term in Eq. (5) will be in a coherent relationship with the direct and specular contributions. Because the range terms R_{1j} and R_{2j} are continuously changing, the total diffuse signal will have a random character with well defined statistical properties (power density vs frequency, correlation coefficient, power density vs delay etc.).

The sum of the three terms given by Eqs. (1), (3) and (5) now provide a direct representation of the total receiver signal. Insofar as the cross-sections σ_{oj} are known, and the areas A_j are appropriately chosen, the representation will possess the same statistical properties as the actual multipath signal. It is difficult to estimate the minimum number of terms in Eq. (5) needed for a statistically valid representation, and this problem is not considered here. In practice, the sizes for A_j are probably most conveniently determined empirically, by reducing their size and increasing their number until the statistics of interest show no significant change. In this report, we will not make use of this direct representation of the total signal, since we calculate only two simple statistics of the multipath signal.

III. THE SYSTEM GEOMETRY

In order to introduce the program for estimating multipath signals, it is necessary first to establish a precise system geometry. This geometry is fixed by the positions of the transmitter T, the moving aircraft P, and the spherical earth, but is a good deal easier to visualize than to specify algebraically. The basic coordinate systems are most conveniently defined (see Fig. 2) by the specular point O, the center of the earth C, and the positions P and T. The specular point is that point on the mean surface of the earth in the plane TPC for which the angle θ_i (THI) between the local vertical CO and the line of sight OP is equal to the angle between CO and OT. An xyz coordinate system with origin O, with z-axis along the local vertical, and with x-axis in the POT plane may now be constructed. The tangent plane at the specular point is then the xy plane. The aircraft is at altitude H above the tangent plane with coordinates

$$\begin{aligned}x_p &= H \tan \theta_i \\y_p &= 0 \\z_p &= H.\end{aligned}$$

The satellite has range R_{1S} (RSAT) from O, with coordinates

$$\begin{aligned}x_s &= -R_{1S} \sin \theta_i \\y_s &= 0 \\z_s &= R_{1S} \cos \theta_i.\end{aligned}$$

The scatter point S on the surface of the earth has coordinates x,y,z, or may be defined by the polar coordinates Re, θ, ϕ (where Re (RE) is the radius of the earth) in the coordinate system x'y'z' with origin at C. In the computer program, variables X, Y define the scatter area center point at S, and the polar coordinates (STHR) $\equiv \sin \theta = (x^2 + y^2)^{1/2} / Re$ and (SPH) $= \phi = \tan^{-1} y/x$ are computed. The distance (ZP) $= (-z) = Re(1 - \cos \theta)$ of the J-th scattering point below the tangent plane, and the ranges

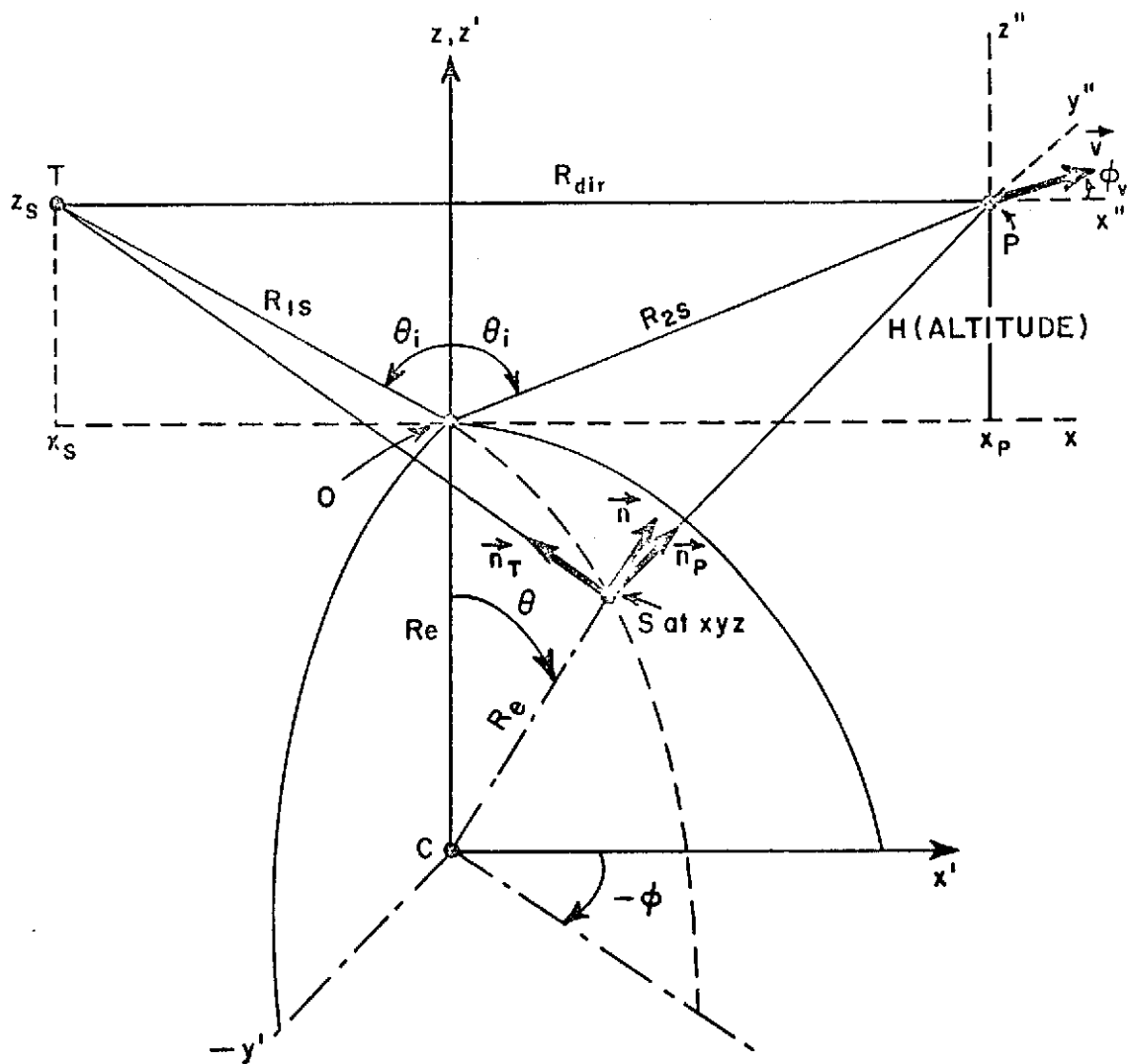


Fig. 2. Multipath geometry.

$$\begin{aligned}
 (6) \quad R_{1j} &= (RS(J)) = ST \\
 R_{2j} &= (R(J)) = SP \\
 R_{dir} &= (REF) = TP \\
 R_{spec} &= (RELSP) = TO+OP
 \end{aligned}$$

are now easily found. Unit vectors \vec{n}_p (along S to P), \vec{n}_T (along S to T) and \vec{n} (the local vertical at S) have components $(CNI(I,J))$, $(CNS(I,J))$ and $(CN(I,J))$ along the $x(I=1)$, $y(I=2)$ and $z(I=3)$ axes respectively.

The aircraft, with position P is at the origin of a second coordinate system x'', y'', z'' parallel to xyz , and is assumed to be moving with velocity \vec{v} in the $x'' y''$ plane, with the velocity vector making an angle ϕ_v (PHV) with the x'' axis.

The antenna patterns are specified as functions of polar angles θ_a , ϕ_a (see Fig. 3) in a polar coordinate system attached to the metal of the aircraft, with polar angle θ_a measured from the z'' axis and azimuth angle ϕ_a measured from the velocity vector.

IV. ANTENNA PATTERNS AND POLARIZATIONS

One must next specify the antenna patterns and polarization states of the transmitter and receiver. For this purpose, it will be assumed that T is sufficiently far from O and P so that the satellite antenna gain and polarization state is uniform over the entire scattering area, including the specular point and the direct path. (Otherwise it would be necessary to introduce still another set of coordinates centered on the transmitter.) Two unit vectors $\vec{i}_{T1} = -\vec{i}_x \cos \theta_1 - \vec{i}_z \sin \theta_1$ and $\vec{i}_{p1} = -\vec{i}_y$ transverse to the line of sight may be used to specify the transmitter polarization via the two complex numbers $A = (ATH)$ and $B = (BPH)$. More precisely, the transmitted electric field in the vicinity of the earth may be written, at range R_1 ,

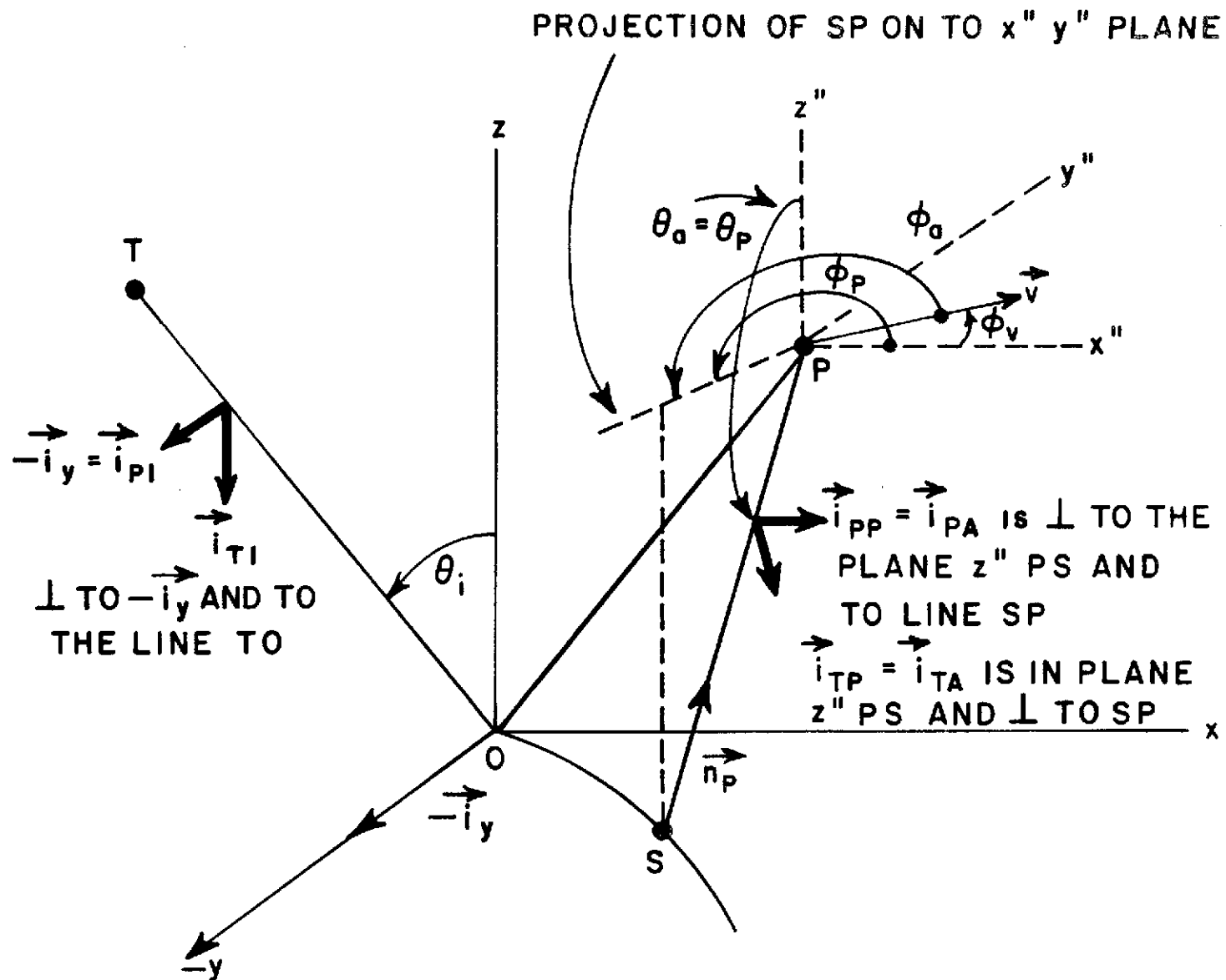


Fig. 3. Polarization unit vectors and antenna pattern coordinates.

$$(7) \quad \vec{E}(x,y,z,t) = \frac{V_0(t-R_1/c)}{R_1} [A\vec{i}_{T1} + B\vec{i}_{P1}]$$

where the complex unit vector \vec{p}_T

$$(8) \quad \vec{p}_T = (A\vec{i}_{T1} + B\vec{i}_{P1})$$

is the transmitter polarization. Since $\vec{p}_T \cdot \vec{p}_T^* = 1$, one must have $AA^* + BB^* = 1$. For example

$$\begin{aligned} A &= (0,0) & B &= (1,0) & \text{"horizontal" polarization} \\ A &= (1,0) & B &= (0,0) & \text{"vertical" polarization} \\ A &= (1/\sqrt{2}, 0) & B &= (0, +j/\sqrt{2}) & \text{"right circular".} \end{aligned}$$

If the transmitter is radiating a cw signal, of angular frequency ω_0 , or frequency f_0 (F), then the reference level voltage is

$$(9) \quad V_0(t) = \left(\frac{P_T G_T Z_0 / 4\pi}{R_1} \right)^{1/2} \exp \left[j\omega_0 \left(t - \frac{R_1}{c} \right) \right]$$

where P_T = transmitted power
 G_T = transmitter antenna gain
 $Z_0 = 120\pi$ ohms.

The receiver antenna is specified by its maximum receiving aperture A_m , its pattern function $f(\theta_a, \phi_a)$ and its polarization state

$$(10) \quad \vec{p}_R(\theta_a, \phi_a) = C(\theta_a, \phi_a)\vec{i}_{TA} + D(\theta_a, \phi_a)\vec{i}_{PA}$$

where again $CC^* + DD^* = 1$, and the unit vectors \vec{i}_{TA} (unit θ_a vector) and \vec{i}_{PA} (unit ϕ_a vector) are shown in Fig. 3. In the x"y"z" system, the polar coordinates defining the line of sight, P to S, are θ_p, ϕ_p with unit vectors $\vec{i}_{TP}, \vec{i}_{PP}$. These two sets are related by

$$\begin{aligned} \theta_a &= \theta_p & \vec{i}_{TA} &= \vec{i}_{TP} \\ \phi_a &= \phi_p - \phi_V & \vec{i}_{PA} &= \vec{i}_{PP} \end{aligned}$$

The receiver complex polarization states $C = (CTH)$ and $D = (DPH)$ are specified in terms of the polarization that the antenna would produce if it were operated as a transmitter. That is, the receiver antenna, if excited by a cw signal, would produce an electric field $E_{ref}[\vec{P}_R]\exp[j\omega_0(t-R/c)]$ in the vicinity of S where E_{ref} is a reference level.

Thus, for example, in direct transmission from satellite to receiver, the receiver voltage would be proportional to

$$V_{rec}(t) = \frac{V_0(t-R_{dir}/c)}{R_{dir}} (\vec{P}_T \cdot \vec{P}_R) \sqrt{f(\theta'_a, \phi'_a)} K$$

where $\theta'_a, \phi'_a = \pi - \phi_v$ are the values of θ_a, ϕ_a in the direction P to T of the transmitter, and K is a proportionality constant related to the receiver gain.

The factor $\vec{P}_T \cdot \vec{P}_R = AC + BD$ is the polarization mismatch factor. For example, for the receiver,

$$\begin{aligned} C &= (0,0) & D &= (1,0) & \text{"horizontal"} \\ C &= (1,0) & D &= (0,0) & \text{"vertical"} \\ C &= (0, j/\sqrt{2}) & D &= (1/\sqrt{2}, 0) & \text{"right circular"} \end{aligned}$$

Thus the polarization mismatch factor between a right circular transmitter ($A = 1/\sqrt{2}, B = j/\sqrt{2}$) and a right circular receiver ($C = j/\sqrt{2}, D = 1/\sqrt{2}$) is $AC + BD = j$; that is, the "right circular" receiver completely absorbs "right circular" incident radiation.

V. THE SCATTERING PROBLEM

Since the intensity of the multipath signal depends on σ_0 , the scattering cross-section per unit area, we next consider scattering model which will provide this parameter. The predominant contribution to the

diffuse energy comes from a series of specular (forward) scatter points; the cross-section for scattering of this type at microwave frequencies is derived from the "optical" or "physical optics" model[4]. In this model, the total cross-section is the product of two factors, the first a polarization transforming reflection coefficient, and the second a probability density function for surface slope. If we consider an element of the mean surface of area $dS = dx dy \sec\theta$, at a point where the local vertical is \vec{n} , then the geometry for specular reflection will be as illustrated in Fig. 4. Those facets in dS which are suitably oriented for specular reflection will have a local normal \vec{n}_0 which is the coplanar bisector of \vec{n}_T and \vec{n}_p . The angle $\theta_n = (TH) = \cos^{-1}(\vec{n} \cdot \vec{n}_0)$ between the local vertical and the normal to the tilted specular facet then determines, from the known slope distribution of the surface, the probability that the facet normals are properly oriented. The angle between the incident polarization vector \vec{P}_T and the vector perpendicular to the plane of incidence $\vec{q} = \vec{n}_p \times \vec{n}_T / |\vec{n}_p \times \vec{n}_T|$ determines the reflection coefficients and polarization transformation.

Thus the computational problem is to determine for each point dS , the voltage response of a polarized receiver due to a plane wave of known polarization and direction which has been reflected by a plane surface of complex dielectric constant ϵ . The subroutine (COEF) determines this in the following manner. Consider (see Fig. 4) a coordinate system ξ, η, ζ with ζ the local vertical and ξ, η , the plane of the mean surface dS . A plane wave is incident from a direction θ_{inc} in the ξ, ζ plane. A scattering direction is defined by polar angles θ_{scat} and ϕ_{scat} . The problem is to find the polar angles θ_n, ϕ_n which define \vec{n}_0 the tilted surface normal required to produce specular reflection from the given incident wave into the chosen scattering direction. The normal clearly lies in the plane of, and bisects the angle TSP. The scattering angle (the angle of incidence in the "plane of incidence" system) is α with $2\alpha = \angle TSP$. The subroutine finds θ_n, ϕ_n and α , given $\theta_{inc}, \theta_{scat}, \phi_{scat}$ by standard trigonometric manipulation. If the incident plane wave has polarization $\vec{P}_T = A \vec{I}_{T1} + B \vec{I}_{p1}$ and the receiver has polarization state

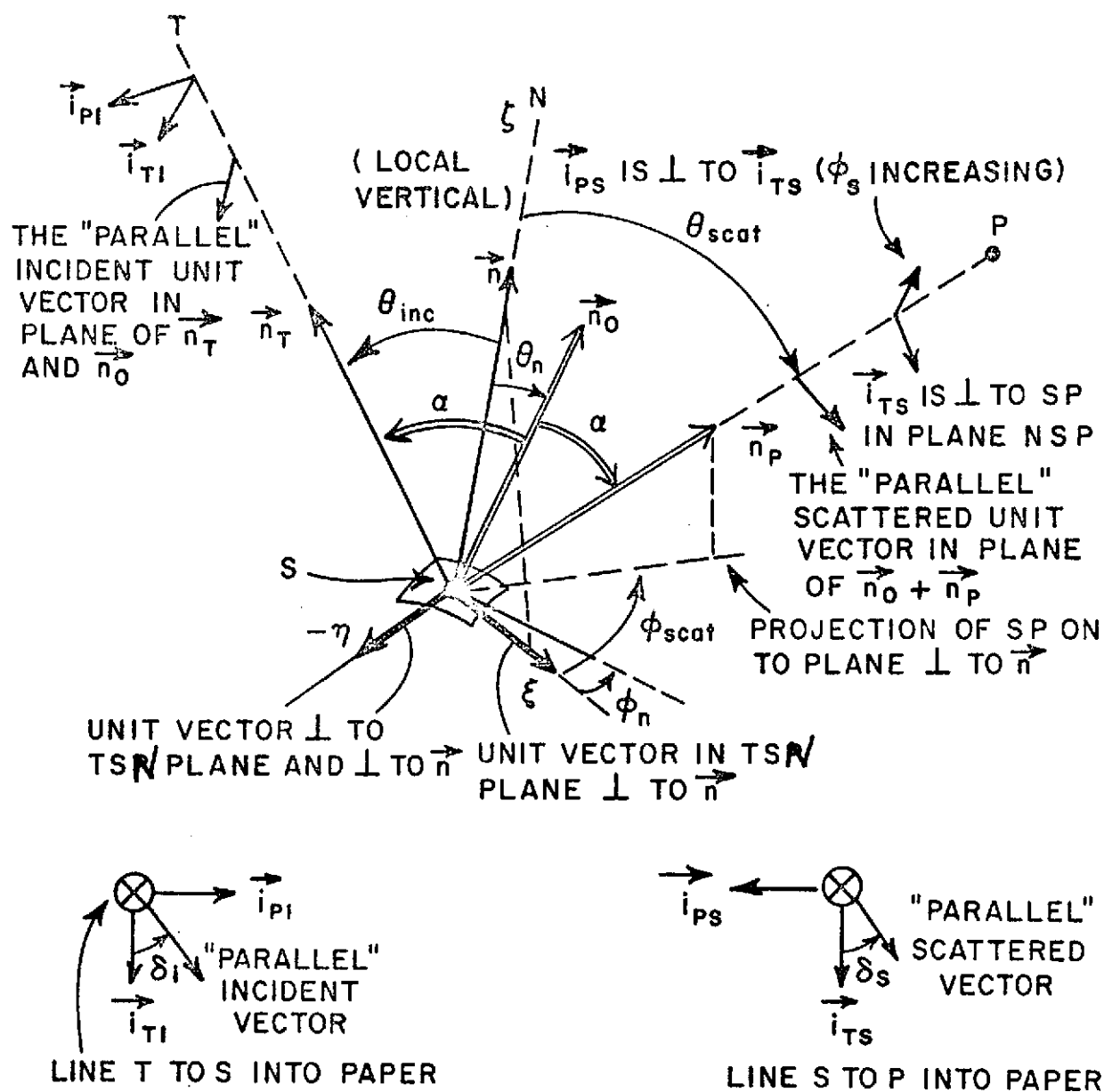


Fig. 4. The scattering coordinate system.

$$(11) \quad \vec{p}_R = C_1 \vec{i}_{TS} + D_1 \vec{i}_{TS}$$

where the unit vectors are as indicated in Fig. 4, then it is simple to show, by resolving \vec{p}_R into components parallel and perpendicular to the plane of incidence, that the effective reflection coefficient and polarization mismatch factor R_{cf} (RCOEF) is

$$(12) \quad R_{cf} = R_{||}(\alpha) [A \cos \delta_i + B \sin \delta_i] [C_1 \cos \delta_s - D_1 \sin \delta_s] \\ - R_{\perp} [B \cos \delta_i - A \sin \delta_i] [D_1 \cos \delta_s + C_1 \sin \delta_s]$$

where

$$(13) \quad R_{||}(\alpha) = (\epsilon \cos \alpha - E) / (\epsilon \cos \alpha + E) \quad (\text{RPAR}) \\ R_{\perp}(\alpha) = (\cos \alpha - E) / (\cos \alpha + E) \quad (\text{RPER}) \\ E = (\epsilon - \sin^2 \alpha)^{1/2}$$

where δ_i (see Fig. 4) is the angle between \vec{i}_{T1} and the incident "parallel" unit vector, and δ_s is the angle between \vec{i}_{TS} and the reflected "parallel" unit vector. (A complete discussion of this simple but tedious problem is given in Ref. 4). Thus the complete subroutine

$$\text{COEF}(\theta_{inc}, \theta_{scat}, \phi_{scat}, \epsilon, A, B, C_1, D_1)$$

accepts calculated values of the calling parameters, and returns α , δ_i , δ_s , θ_n , ϕ_n and R_{cf} . The only problem remaining in the use of the subroutine is the connection between the scatter geometry of Fig. 4, and the system geometry of Fig. 3. By comparing these figures it is clear that $\vec{i}_{TS} = \vec{i}_{TP}$ and $\vec{i}_{PS} = -\vec{i}_{PP}$. In the program, this is accounted for by changing the sign of D, i.e., $C_1 = C$ and $D_1 = -D$ (DPHI = -DPH). Notice also that a slight error (entirely negligible for satellites in stationary orbits) is incurred in the program by assuming that the incoming wave polarization vectors do not depend on the scatter point position.

VI. THE RECEIVED POWERS

With the coordinates and scattering parameters defined, we are now in a position to compute the relative power level, the doppler shift, and the time delay in each of the three transmission paths.

A. The Direct Power

The direct power received by the aircraft from a distant satellite is simply

$$(14) \quad P_{\text{dir}} = \frac{P_{\text{T}} G_{\text{T}} A_{\text{m}}}{4\pi R_{\text{dir}}^2} f(\theta_{\text{i}}, \pi - \phi_{\text{v}}) |AC + BD|^2$$

$$C = C(\theta_{\text{i}}, \pi - \phi_{\text{v}})$$

$$D = D(\theta_{\text{i}}, \pi - \phi_{\text{v}})$$

except for a small error in the mismatch factor due to the finite range of the satellite. The direct signal is received at a frequency $f_0 + f_{\text{dir}}$, where f_{dir} is the doppler shift,

$$(15) \quad f_{\text{dir}} = - \frac{\vec{v} \cdot \vec{n}_{\text{d}}}{c} f_0 \quad (\text{DDD})$$

and f_0 is the carrier frequency. The direct path doppler is printed out in H_z , a positive doppler indicating the received frequency is higher than the transmitter carrier frequency. In the program, the direct power is computed relative to a reference power level, namely that received by a polarization matched receiver at the specular point. That is, the direct power is calculated and printed as

$$(16) \quad \text{PDIR} = (R_{\text{ls}}/R_{\text{dir}})^2 |AC + BD|^2 f$$

so that the actual direct power in watts is

$$(17) \quad P_{\text{dir}} = (P_{\text{T}} G_{\text{T}} A_{\text{m}} / 4\pi R_{\text{ls}}^2) \cdot (\text{PDIR}) .$$

The time delay on the direct path is taken to be zero, so that all other delays are relative to the direct path delay.

B. The Coherent (Specular) Reflected Power

The magnitude of the specular path power is less than the direct path mainly because of the surface roughness (Rayleigh Factor) but also because of the reflection coefficient and the slightly longer path length. In the program the specular power is computed as

$$(18) \quad \text{PSPEC} = (R_{1s}/R_{\text{spec}})^2 f(\pi-\theta_i, \pi-\phi_v) |R_{cf}|^2 \exp(-2(kh \cos \theta_i)^2)$$

where

$$R_{cf} = \text{RCOEF}(\theta_i, \theta_i, 0, \epsilon, A, B, C, D_1)$$

$$C = C(\pi-\theta_i, \pi-\phi_v)$$

$$D_1 = -D(\pi-\theta_i, \pi-\phi_v)$$

so that again the actual specular power in watts is

$$(19) \quad P_{\text{spec}} = (P_{TTm} G_A / 4\pi R_{1s}^2) \cdot (\text{PSPEC}).$$

However, the value of PSPEC printed out is the ratio $10 \log (P_{\text{spec}}/P_{\text{dir}})$ i.e., it is the ratio of specular to direct (not reference) power in decibels. This is a more significant ratio than the actual specular power for system studies. At L-band, P_{spec} is negligible except for very smooth seas, or near grazing incidence.

The specular doppler shift is given by

$$(20) \quad f_{\text{spec}} = - \frac{\vec{v} \cdot \vec{n}_{sp}}{c} f_0 \quad (\text{DDO})$$

and is printed out in Hz. It is almost identical to the direct doppler. The time delay of the specular path power is calculated from

$$(21) \quad \tau_{sp} = \text{DELS} = (R_{1s} + R_{2s} - R_{\text{dir}})/c$$

and is printed out in microseconds.

C. The Diffuse Power

The program computes the diffuse power by dividing the xy plane into squares of side dx(DX) and dy(DY) centered at $x = (J + 1/2)dx$, $y = (K + 1/2)dx$ (J,K integers). Each square is then projected onto the spherical earth surface, for which the actual area becomes $dx dy / \cos \theta$. The width of the square is taken as

$$dx = \left(\frac{\eta}{JJJ} \right) \frac{2H}{\cos^2 \theta_i}$$

where JJJ is an integer of order 20 to 35. This choice of square size ensures a smaller integration area for surfaces of small root mean square slope η . The incremental power scattered by this area and absorbed by the receiver is then given by

$$(22) \quad dP(J,K) = \frac{P_T G_T A_m}{4\pi R_{1j}^2} \cdot f(\theta_a, \phi_a) \sigma_{oo} \frac{|R_{cf}|^2 dx dy}{4\pi R_{2j}^2 \cos \theta}$$

where σ_{oo} is the scattering cross-section per unit area of a perfectly conducting rough surface, and R_{cf} accounts for the reflection coefficient of the actual surface, and receiver polarization mismatch. The scattering cross-section for the sea surface, based on the physical optics model, is given by[4]

$$(23) \quad \sigma_{oo} = \pi \sec \theta_n P(\theta_n, \phi_n)$$

where θ_n, ϕ_n are polar angles of the normal \vec{n}_o required for reflection (see Fig. 4). Here $p_n(\theta_n, \phi_n)$ is the probability density function for the surface normal \vec{n}_o , i.e., $p(\theta_n, \phi_n) d\Omega_n$ is the probability that the normal lies in the cone of solid angle $d\Omega_n = \sin \theta_n d\theta_n d\phi_n$. For the sea surface the actual slope distribution is a rather complicated function of the wind velocity and its history[5]. For the purposes of this report it is sufficient to assume the rather simple isotropic form

$$(24) \quad p(\theta_n, \phi_n) = \frac{\cos \theta_n}{\pi \eta^2} e^{-\frac{\tan^2 \theta_n}{\eta^2(1+2\eta^2)}} \quad (\text{PDEN})$$

where η^2 = mean square surface slope
 $= \langle \tan^2 \theta_n \rangle$ (average value of $\tan^2 \theta_n$ over surface).

This form is quite similar to a cross-wind section of the standard (Cox-Munk) distribution[5] and, for surfaces of moderate slope, very nearly satisfies the normalization conditions

$$(25) \quad \begin{cases} \int P(\theta_n, \phi_n) d\Omega_n = 1 \\ \int P(\theta_n, \phi_n) \tan^2 \theta_n d\Omega_n = \eta^2 \end{cases}$$

Consistent with the power normalization used for the direct power, the normalized power increment (DP) is computed as

$$(26) \quad DP = f(\theta_a, \phi_a) |R_{cf}|^2 \frac{e^{-\tan^2 \theta_n / \eta^2 (1+2\eta^2)}}{\pi \eta^2} \frac{dx dy}{R_{2j}^2 \cos \theta} \left(\frac{1}{4}\right)$$

so that the actual incremental power in watts is

$$(27) \quad dP = DP [P_t G_t A_m / 4\pi R_{1s}^2].$$

(It will be noted that a small error is incurred in Eq. (26) because the transmitter to surface distance is assumed to be R_{1s} at all times, instead of the variable R_{1j} . For satellites in stationary orbit the difference between Eq. (26) and the correct power level is insignificant.) The doppler and delay for this element, as before, are given by

$$(28) \quad \begin{cases} f_{diff} = - \frac{\vec{n}_p \cdot \vec{v}}{c} f_o \\ \tau_{diff} = (R_{1j} + R_{2j} - R_{dir})/c \end{cases}$$

In the actual program, the incremental powers are calculated for four cells (at $\pm x$, $\pm y$) at a time, beginning with the four cells nearest the specular point. These four cells determine a reference power level (DPI). The subsequent sets are obtained by increasing $|x|$ with $|y|$ constant until the power from a set is less than some predetermined fraction of the power found in the first set. (1/1000 in the program of Appendix I.) At this point y is incremented, x returned to zero and the process repeated until further increase in y fails to produce sufficient power to satisfy the above condition. At this point the iteration stops, and the maximum values of x (XMAX) and y (YMAX) are printed. The values XMAX and YMAX then define an ellipse within which all significant scattering occurs.

As the power from each set is computed, the doppler shift and the time delay for the path is also found, and the incremental power assigned to a doppler or delay bin. In this program 128 doppler bins cover the range of $2v/c f_o$, the maximum possible range of doppler frequencies. The delay bins are 2 nanoseconds wide. Thus one can determine the doppler spectrum, (the power per Hz vs frequency) and the delay spectrum. In addition, the total diffuse power (PT), the sum of the power in all bins, is calculated in dB below the direct power.

$$(29) \quad PT = 10 \log(\text{Total Diffuse Power}/P_{\text{dir}}).$$

VII. THE PROGRAM PARAMETERS

To utilize the program, listed in Appendix I; a number of parameters must be specified. These are:

A. Ocean Temperature and Salinity

- TEM The temperature of the ocean in °C.
- SAL The salinity of the ocean in parts per thousand.
(Typically SAL = 35 ppt.)
- F The carrier frequency in GHz.

These three parameters determine the complex dielectric constant of the ocean via the complex function (EPS). This subroutine calculates ϵ according to the formula given by Stogryn in Reference [6]. The frequency F should probably be limited to the range 0.4 GHz < f < 5 GHz in order for the ocean scatter mechanism to be valid.

B. Ocean Slope and Roughness

ANG is the root mean square slope of the ocean in degrees.

RUF is the root mean square height of the ocean in meters.

In terms of the report variables, $ANG = (180/\pi)\tan^{-1}\eta$ and $RUF = h$. These two oceanographic parameters may be chosen in a number of obvious ways. For many types of calculation however, it is convenient to relate them to a single variable, the wind speed W over the ocean. Thus, for example one may modify a standard[5] expression for the mean square slope of the ocean surface to obtain

$$(30) \quad \eta^2 \approx 0.006 \ln(K_m/K_{oc}).$$

$$K_{oc} = g/W^2$$

$$g = \text{Acceleration of Gravity} = 9.81 \text{ m/sec}^2$$

$$K_m = \gamma k = \gamma 2\pi/\lambda$$

$$\lambda = \text{electromagnetic wavelength}$$

$$\gamma = \text{empirical constant} \approx 4$$

where K_{oc} is the wave number for the largest ocean waves developed at a wind velocity W and K_m is the wave number for the smallest ocean waves that are effective in the electromagnetic scattering process. That is, expressions for the mean square slope in the oceanographic literature are based on the actual ocean surface, including many small waves (ripples) superimposed on the large scale wave structure. These small scale waves do not participate in the forward scattering process and thus the effective mean square slope is smaller than the oceanographic value. The estimate

$K_m = 4 k$ is an empirical result which should be valid for frequencies up to 5 GHz and moderate to large wind velocities. Similarly, the roughness may be estimated from

$$h^2 = .003/K_{OC}^2 = .003 W^4/g^2$$

$$h = .055 W^2/g \text{ meters}$$

for wind velocities greater than a few meters/second.

C. Aircraft Velocity

VEE = aircraft speed in meters/sec

PHV = angle of velocity vector from x-axis in degrees.

Thus when PHV = 0 the aircraft is flying directly away from the satellite.

D. Geometry of Path

THI = angle of incidence at the specular point in degrees

H = aircraft altitude above x,y plane in meters.

E. Antenna Polarization and Patterns

ATH, BPH Two complex numbers defining the polarization state of the transmitting antenna.
(A, B in report)

CTH(θ_a, ϕ_a) Two complex functions defining the polarization state of the receiving antenna
DPH(θ_a, ϕ_a)
(C, D in report)

ANTP(θ_a, ϕ_a) Antenna power pattern function $f(\theta_a, \phi_a)$ in report.

In the program in Appendix I, the antenna power pattern $f(\theta_a, \phi_a)$ is taken as isotropic, i.e., $f = 1$. The two functions C and D are also taken as constants, i.e., the polarization of the receiver is independent of look direction.

F. Integration Parameter

JJJ = an integer defining increment in x.

If JJJ is taken too small, (say less than 10), the density and delay spectra appear erratic because the elementary areas are too large. If JJJ is too large, (say greater than 40) the running time becomes prohibitive. Reasonable values appear to lie in the range $20 < JJJ < 30$.

G. Program Output

The output of the program, an example of which is given in Appendix II, are the direct power, the specular power in dB and the total diffuse power in dB; the specular and direct doppler shifts; the specular delay; and the bin widths of the doppler and delay spectra. Note that the unshifted carrier frequency is always in bin 65, and that the bin which would contain the direct and specular returns is also indicated. The complex dielectric constant is printed out as EPS.

The graphical output consists of two graphs, one of power per doppler bin vs doppler bin number, and the other of power per delay bin vs delay bin number. The widths of the doppler and the delay bins are indicated. The total power in the doppler spectrum should sum to the output diffuse power level when converted to dB.

Note that the diffuse and specular power are stated in dB "below" the direct power. However a negative number indicates that the specular or diffuse power is smaller than the direct power. Note also that when the receiver is blind to the direct power (right circular transmitter to left circular receiver, for example) the direct power is zero, so that the program must be modified if the specular or diffuse power is desired for this case.

VIII. RESULTS AND CONCLUSIONS

Although the purpose of this report is to document the program of Appendix I, and to provide, through Eqs. (1), (3) and (5) convenient realizations of the multipath signal, a number of cases have been run to illustrate the principal features of the diffuse multipath spectra.

In Fig. 5, the doppler spectrum is plotted vs doppler bin for several values of ϕ_v , the aircraft flight direction. In each graph the location of the specular power is shown. Evidently, the spectra tend to be centered on the specular signal, indicating that the major part of the diffuse power is emanating from a scattering region near the specular point. Figure 6 indicates the effect of increasing the surface roughness (mean square slope) on the shape and intensity of the scattered signal. Notice that for aircraft velocities nearly along the line of sight, the spectra are skewed towards the extreme doppler bins, especially for the rough surfaces. Note also a tendency for the diffuse power to saturate as the mean square slope increases. Figure 7 illustrates the variation of doppler spectrum as the angle of incidence is varied, and Fig. 8 shows the effect of polarization on the spectrum, and on the direct and diffuse total power. Clearly an appropriate choice of transmitter and receiver polarization can significantly influence the character of the total signal. Figure 9 shows several typical delay spectra and illustrates the fairly rapid initial decay and the extended tail echo for certain geometries. Note that in the program, the power in delay bins beyond the hundredth has been accumulated in the last bin.

It may be concluded that the program of Appendix I provides a convenient means for estimating a number of features of the multipath signals which occur when a satellite to aircraft link is maintained over the ocean. It should be possible to undertake the study of a variety of detectors using either the statistical signal properties given by the program, or the signal realization given in Section II. In situations where standard detection schemes must be used, the program may be easily modified to investigate the feasibility of multipath rejection by antenna pattern or polarization control.

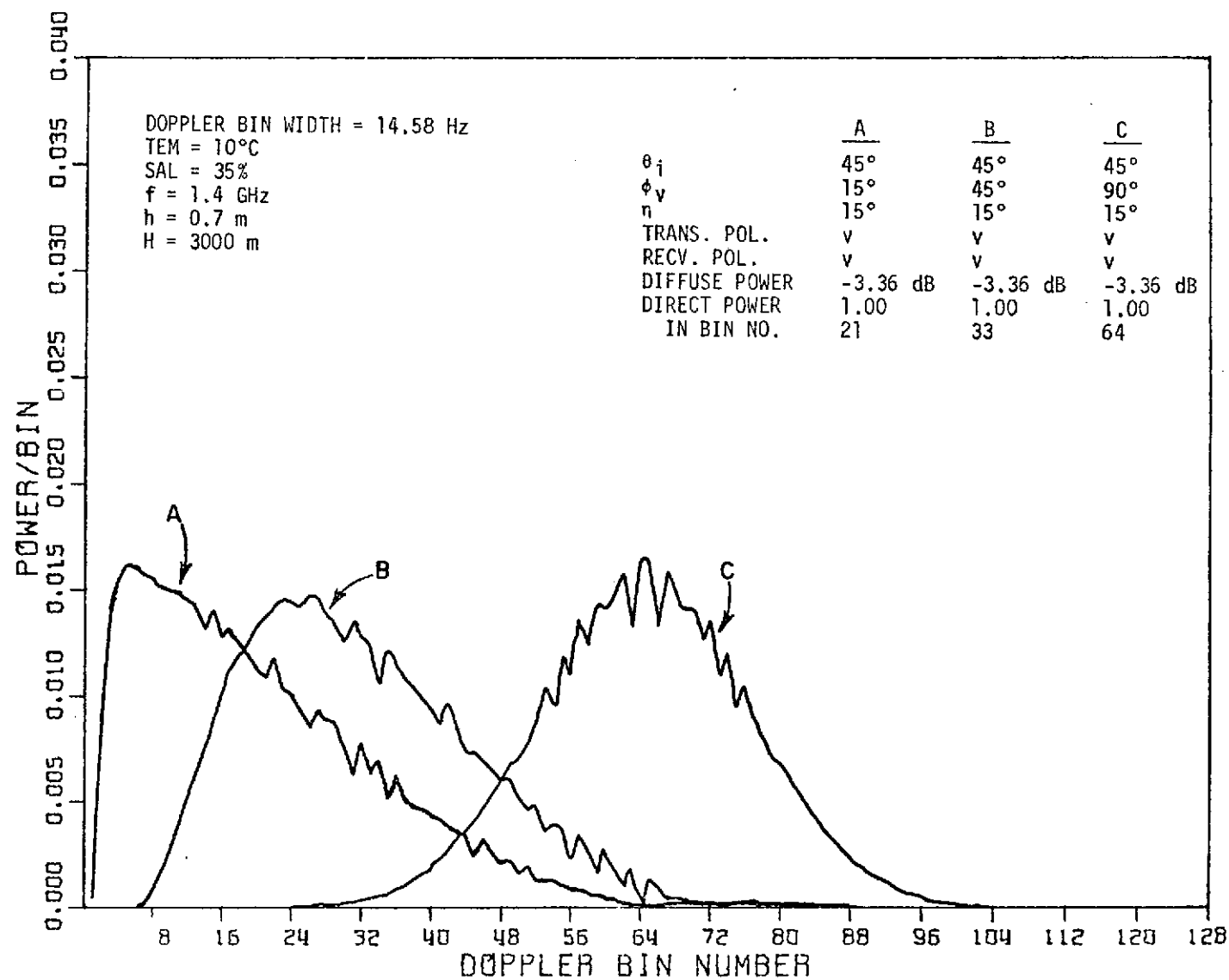


Fig. 5. Doppler spectrum with aircraft direction as parameter.

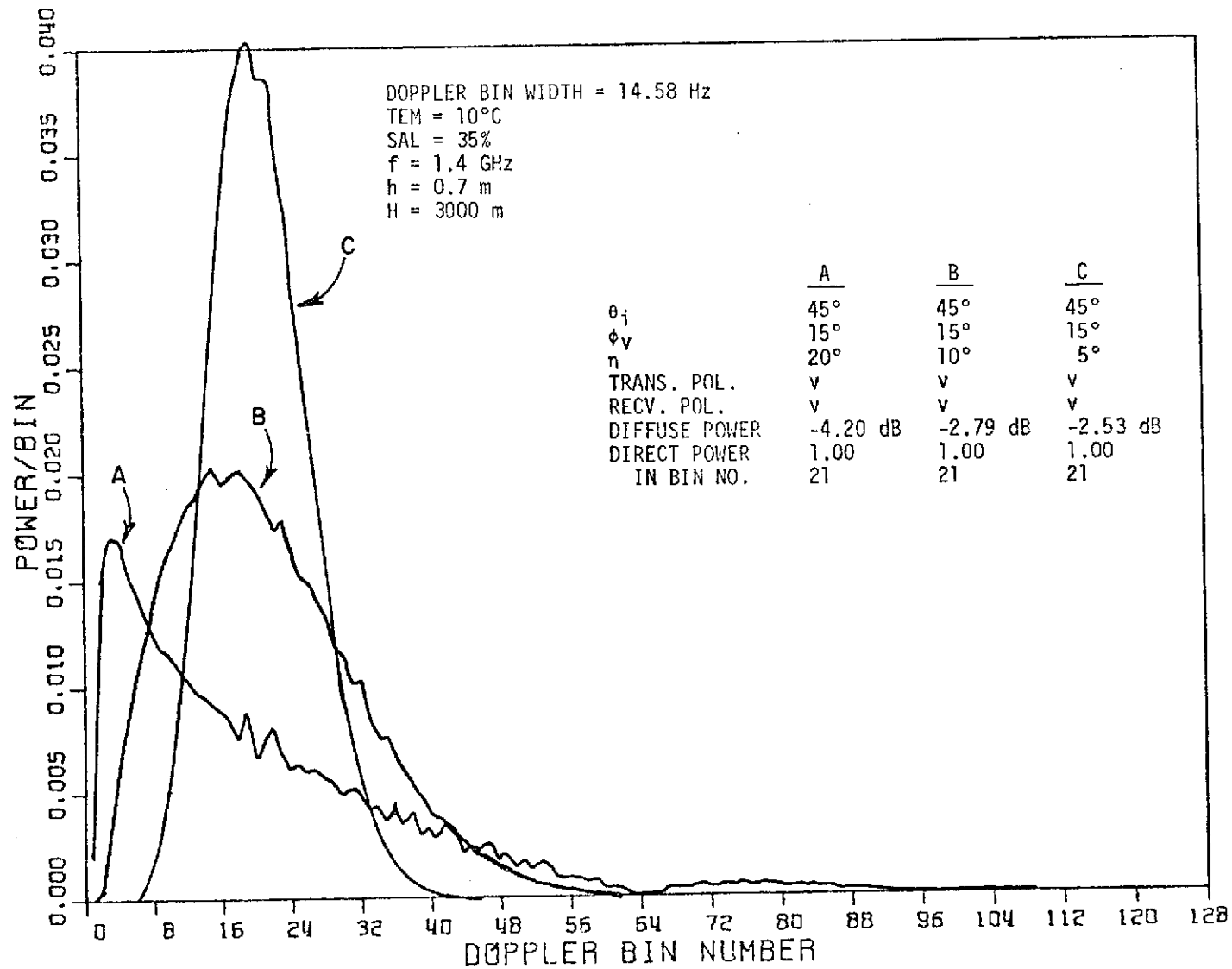


Fig. 6. Doppler spectrum with surface slope as parameter.

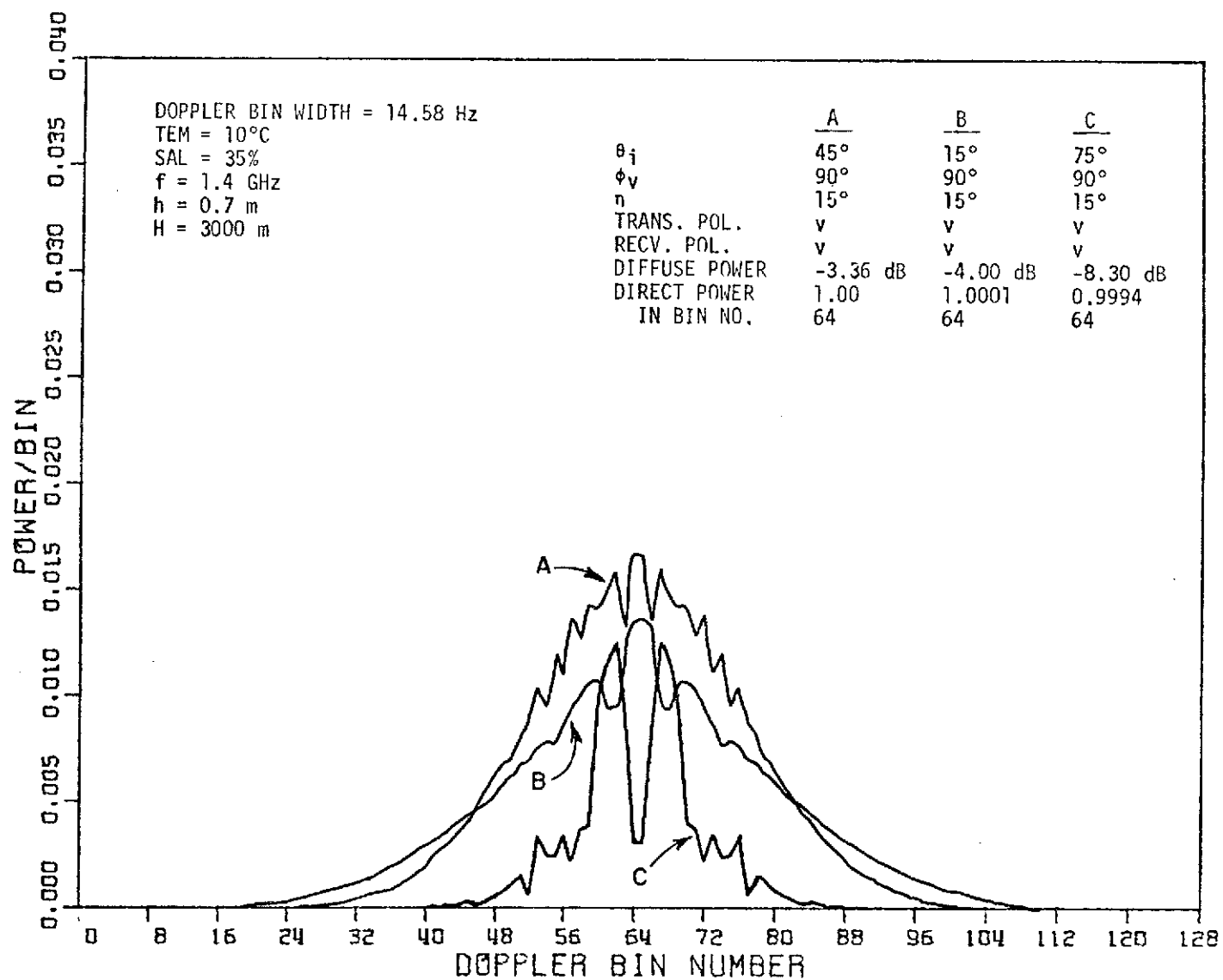


Fig. 7. Doppler spectrum with angle of incidence as parameter. The oscillation in curve C between bins 58 and 70 is an artifact of the program, and illustrates the effect of choosing JJJ too small.

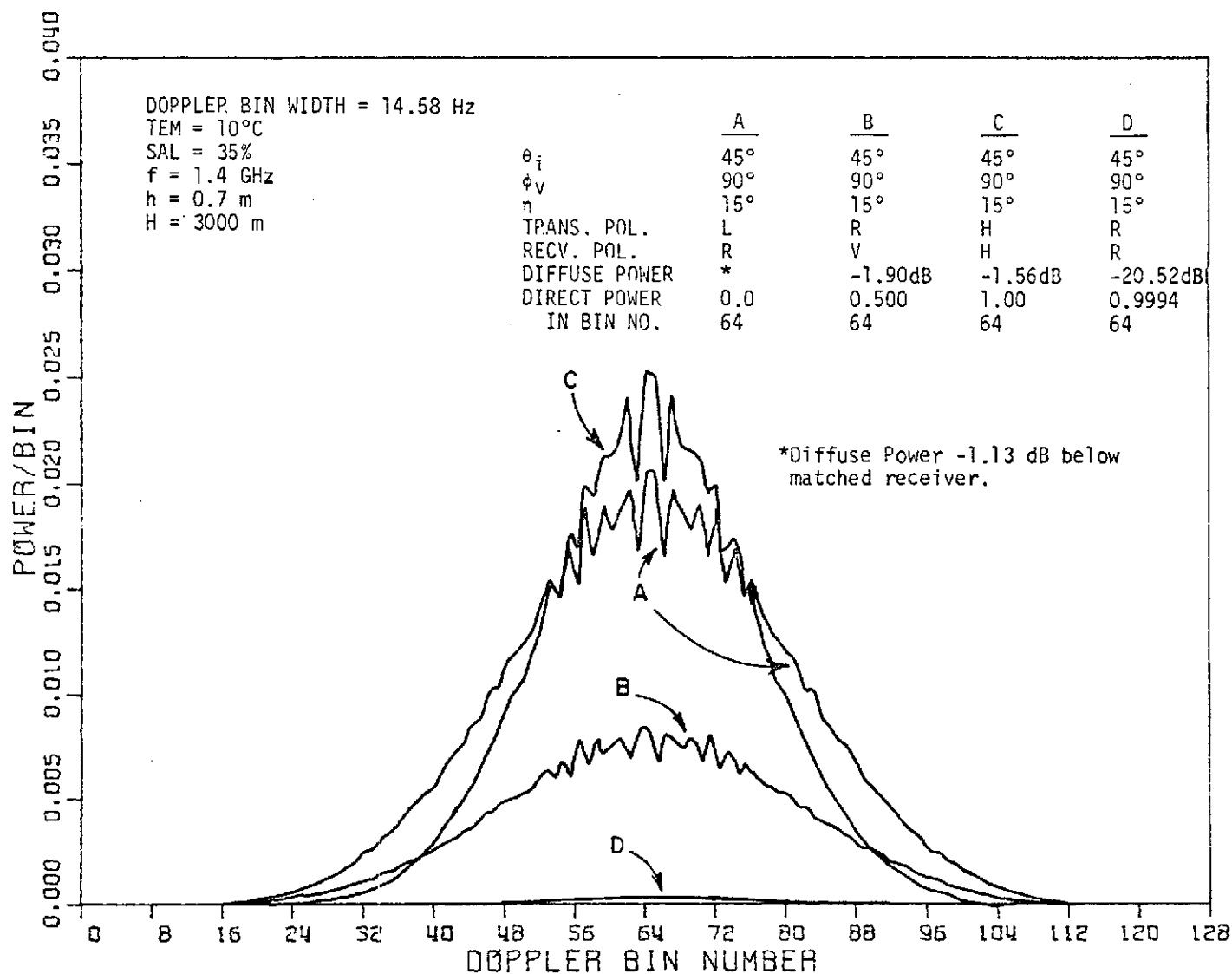


Fig. 8. Doppler spectrum with polarization as parameter. Note that the diffuse power in curve B is -1.90 dB below the direct power of 0.5, or -4.90 dB below a polarization matched receiver.

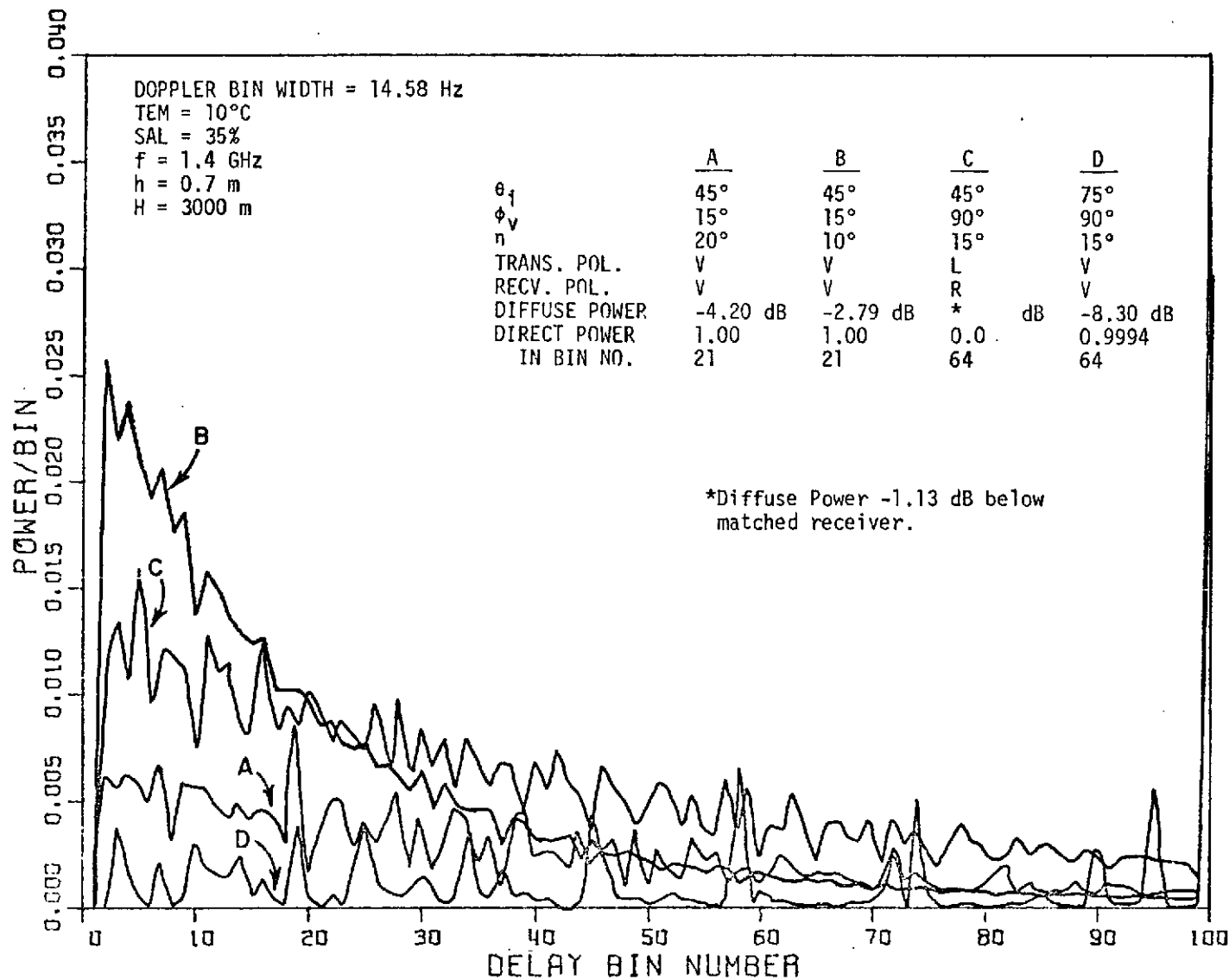


Fig. 9. Delay spectrum for various geometries. The delay bin width is 2 nanoseconds. A time delay of 0 (bin 1) is coincident with the specular signal, i.e., 14.1413 microseconds later than the direct signal for this geometry.

APPENDIX I

```

1 C      THIS PROGRAM GIVES THE POWER SPECTRAL DENSITY AND TOTAL
2 C      *POWER IN THE DIFFUSE MULTIPATH SIGNAL FROM SATELLITE
3 C      *TO AIRCRAFT OVER THE OCEAN, AND DISTRIBUTION OF POWER
4 C      *VERSUS TIME DELAY
5          DIMENSION SPH(4),RS(4),CN(3,4),CNI(3,4),CNS(3,4),STH(4)
6          DIMENSION CTH(4),CTHS(4),CTHR(4),STHS(4),CPHS(4),SPHS(4)
7          DIMENSION PEEL(250),DEL(4)
8          DIMENSION PR(250),R(4),PHS(4),DP(4),FR(4),YY(2)
9          COMPLEX EP,EPS,RCOEF,ATH,BPH,CTH,DPH,DPH1
10         50 FORMAT(10X,'TEM(C)=',F6.3,5X,'SAL(PPT)=',F6.3,5X,'F(GHZ)=',F6.3,
11         *5X,'SEA SLOPE(DFG)=',F5.2,5X,'SEA HEIGHT=',F5.2,'M')
12         51 FORMAT(10X,'THETA INC=',F8.4,5X,'PHI(PLANE VFL)=',F8.4,
13         *5X,'PLANE HEIGHT(M)=',F12.6,5X,'VELOCITY=',F8.4,'M/S')
14         52 FORMAT(10X,'EPS=',2F10.2,' J')
15         53 FORMAT(//,30X,'GRAPH OF POWER SPECTRUM      BIN WIDTH IS',F8.4,'HZ')
16         54 FORMAT(22X,I3,11X,F12.6)
17         55 FORMAT(//,10X,'DIFFUSE POWER IS',F8.4,'DB; COHERENT POWER IS'
18         *F10.4,' DB BELOW DIRECT POWER OF ',F9.5,)
19         56 FORMAT(//,10X,'MAX VALUES OF X AND Y IN INTEGRATION',5X,'XMAX=',
20         *F12.6,5X,'YMAX=',F12.6,'      DELTX = ',F10.4)
21         57 FORMAT(10X,'ATH=',2F8.4,5X,'BPH=',2F8.4,5X,'CTH=',2F8.4,5X,
22         *'DPH=',2F8.4)
23         58 FORMAT(//,10X,'FINITE RANGE CASE',5X,'JJJ IS ',I3)
24         61 FORMAT(//,30X,'POWER VS DELAY; SPECULAR DELAY IS',F8.4,'MICROSEC')
25         62 FORMAT(//,30X,'SPEC POINT IN BIN 2; BIN WIDTH IS ',I3,' NANOSEC')
26         64 FORMAT(//,10X,'DIRECT DOPPLER IS ',F10.3,' HZ;
27         *SPECULAR DOPPLER IS ',F10.3,' HZ IN BIN ',I3)
28 C
29 C
30 C      INPUT DATA; TEM IS SEA TEMPERATURE IN DEG CENTIGRADE
31 C      SAL IS SALINITY IN P.P.THOU. 35 IS TYPICAL
32 C      ANG IS RMS SLOPE OF SURFACE IN DEGREES 15 IS TYPICAL
33 C      RUF IS RMS ROUGHNESS HEIGHT OF OCEAN IN METRES
34 C
35 C      F IS CARRIER FREQUENCY IN GIGAHZ
36 C      H IS HEIGHT OF AIRCRAFT ABOVE SURFACE IN METRES
37 C      VEE IS AIRCRAFT VELOCITY IN METRES/SEC
38 C      PHV IS ANGLE OF VELOCITY FROM X AXIS; PLANE RECEDING IF PHV=0
39 C      THT IS ANGLE OF INCIDENCE IN DEGREES 1 90 DEG IS GRAZING
40 C      JJJ GIVES FINENESS OF INTEGRATION  JJJ=30 IS TYPICAL
41 C      RE IS RADIUS OF EARTH IN METRES
42 C      RSAT IS DISTANCE FROM SATELLITE TO SPECULAR POINT IN METRES
43 C      ATH,BPH,CTH,DPH ARE COMPLEX POLARIZATION STATES; SEE LATER COMMENT
44 C
45 C
46         READ(8,-)TEM,SAL,F,ANG,VEE,RUF
47         READ(8,-)THI,PHV,H,JJJ
48         READ(8,-)ATH,BPH,CTH,DPH
49 C
50 C
51         PI=3.14159265
52         RE = (20./PI)*1.E6
53         RSAT = 3.5E7
54         WRITE(6,50) TEM,SAL,F,ANG,RUF
55         WRITE(6,51) THI,PHV,H,VEE

```

```

56      WRITE(6,57) ATH,BPH,CTH,DPH
57      WRITE(6,58) JJJ
58 C
59 C
60      ETA2=TAN(ANG*PI/180.)**2
61 C      INITIALIZE STORAGE BINS
62      DO 42 IK=1,250
63      PU(IK)=0.0
64      PUEL(IK) = 0.0
65      42 CONTINUE
66      PT=0.0
67      XP=H*TAN(THI*PI/180.)
68      ZS = COS(THI*PI/180.)*RSAT
69      XS = -SIN(THI*PI/180.)*RSAT
70      REF = SQRT((XP-XS)**2 + (ZS-H)**2)
71      IDX = 2
72      RELSP = RSAT + SQRT(XP**2 + H**2)
73      DELSP = (RELSP - REF)/300.
74      HZ=H*H
75 C
76 C      INCIDENT POLARIZATION DATA
77 C      ATH IS THETA COMPONENT OF SATELLITE POLARIZATION THE THETA UNIT
78 C      VECTOR IS -IX*COS(THI) -IY*SIN(THI); BPH IS PHI COMPONENT WITH
79 C      PHI UNIT VECTOR ALONG -IY; ATH*ATHCONJ +BPH*BPHCONJ = 1.0
80 C      VERT POL ATH=(1.0) BPH=(0.0);HORIZ POL ATH=(0.0) BPH =(1.0)
81 C      RIGHT CIRC POL HAS ATH = (.707,0) BPH = (0,.707) .
82 C
83 C      CALCULATE COMPLEX DIELECTRIC CONSTANT OF SEA WATER
84      EP=EPS(F,TEM,SAL)
85      WRITE(6,52) EP
86 C
87 C      CALCULATE INCREMENTAL AREA
88      DTH=SQRT(ETA2)/JJJ
89      DX=2.*H*DTH/COS(THI*PI/180.1)**2
90      DY=DX
91      XXMAX=0.0
92      YYMAX=0.0
93 C      INTEGRATION STARTS
94      Y=-DY/2.
95      IA=1
96      30 CONTINUE
97      Y=Y+DY
98      IF(Y.GT.YYMAX) YYMAX=Y
99      YZ=Y*Y
100     X=DX/2.
101     31 CONTINUE
102     IF(X.GT.XXMAX) XXMAX=X
103 C      TRUE POLAR COORDINATES OF SCATT POINT ON SPHERICAL EARTH
104     STHR = SQRT(X*X+Y*Y)/RE
105     CTHR = SQRT(1. - STHR**2)
106     THR = ATAN(STHR/CTHR)
107 C      ZP IS DISTANCE OF SCATTER POINT BELOW TANGENT PLANE
108     ZP = RE*2.*SIN(THR/2.)**2
109     DO 99 J = 1,4
110     XU = X

```

```

111      IF( J .GE. 3)   XJ = -X
112      YJ = Y
113      IF( J .EQ. 1 .OR. J .EQ. 3)   YJ = -Y
114      SPH(J) = ATAN2(YJ,XJ)
115      R(J) = SQRT((H+ZP)**2 + YJ**2 + (XJ-XP)**2)
116      RS(J) = SQRT((XJ-XS)**2 + YJ**2 + (ZS+ZP)**2)
117      CN(1,J) = SINH*COS(SPH(J))
118      CN(2,J) = SINH*SIN(SPH(J))
119      CN(3,J) = CTHR
120      CNI(1,J) = (XP-XJ)/R(J)
121      CNI(2,J) = -YJ/R(J)
122      CNI(3,J) = (H+ZP)/R(J)
123      CNS(1,J) = (XS-XJ)/RS(J)
124      CNS(2,J) = -YJ/RS(J)
125      CNS(3,J) = (ZS+ZP)/RS(J)
126      CTHI(J) = 0.
127      CTHS(J) = 0.
128      CTHB(J) = 0.
129      STHS(J) = 0.
130      DO 77 K = 1,3
131      CTHI(J) = CN(K,J)*CNI(K,J) + CTHI(J)
132      CTHS(J) = CN(K,J)*CNS(K,J) + CTHS(J)
133      CTHB(J) = CNI(K,J)*CNS(K,J) + CTHB(J)
134 77  CONTINUE
135      STHS(J) = SQRT(1. - CTHS(J)**2)
136      STHI(J) = SQRT(1. - CTHI(J)**2)
137      IF (ABS(STHS(J)) .LE. .001 .OR. ABS(STHI(J)) .LE. .001) GO TO 78
138      CPHS(J) = (CTHI(J)*CTHS(J) - CTHB(J))/(STHS(J)*STHI(J))
139      SPHS(J) = -(YJ/APS(YJ))*SQRT(1. - CPHS(J)**2)
140      PHS(J) = ATAN2(SPHS(J),CPHS(J))
141      GO TO 99
142 78  PHS(J) = 0.
143 99  CONTINUE
144 C   CALCULATION OF INCREMENTAL POWERS STARTS
145 C   DO 40 II=1,4
146 C   PHSCAT =PHS(II)*180./PI
147 C   THINC = ATAN(SQRT(1.-CTHS(II)**2)/CTHS(II))*180./PI
148 C   THSCAT = ATAN(SQRT(1.-CTHI(II)**2)/CTHI(II))*180./PI
149 C
150 C   THE ANTENNA PATTERN ANTP(THA,PHA) IS A FUNCTION OF THE POLAR COORDINATES
151 C   THA AND PHA FIXED IN THE AIRCRAFT. THE POLAR AXIS IS Z(VERTICAL)
152 C   AND THE X-Y AXIS IS ALONG THE VELOCITY VECTOR, FROM WHICH
153 C   THE ANGLE PHA IS MEASURED. THE ANTENNA POLARIZATION IS GIVEN AS TWO
154 C   COMPLEX FUNCTIONS OF THA,PHA. FUNCTION CTH(THA,PHA) IS THE THETA
155 C   COMPONENT AND DPH IS THE PHI COMPONENT. CTH*CTHCONJ+DPH*DPHCONJ=1
156 C   VERT POL RECVR HAS C=(1,0) D=(0,0); HORIZ POL RECVR HAS C=(0,0)
157 C   D=(1,0); RIGHT CIRC POL RECVR HAS C=(0,.707) D=(+.707,0)
158 C   THA = 180. - THINC
159 C   PHA = PHSCAT - 180. -PHV
160 C   ANTP = 1.0
161 C   THE NEXT LINE CONVERTS UNIT VECTORS FROM AIRCRAFT TO SCATTER COORDS
162 C   DPH1=-DPH
163 C
164 C   CALL COEF(THINC,THSCAT,PHSCAT,EP,ATH,BPH,CTH,DPH1,
165 C   *AL,TH,PH,DELI,DELS,RCOEF)

```

```

166      DP(II)=ANTP*CARB(RCOEF)**2*PDEN(TH,PH,ETA2)*DX*DY/(4.*R(II)*CTHR*
167      *R(II))*COS(TH*PI/180.))
168 C      DOPPLER SHIFT IN HZ FROM CARRIER IS FO*(F*1.E9)*(V/C)
169      FO(II)=-SIN(THSCAT*PI/180.)*COS((PHSCAT-PHV)*PI/180.)
170 C      DELAY IN MICRO SEC REFERRED TO DIRECT PATH
171      DEL(II) = (R(II)+RS(II)-RELSP)/(300.*DELSP)
172 40 CONTINUE
173      IF(IA.EQ.1) DP1=DP(1)
174      IF(IA.EQ.1) IA=YA+1
175 C
176 C      CALCULATE BIN STORAGE OF POWER; 2**7 BINS NUMBERED 1 TO 129
177      PAVG=0.0
178      DO 41 IJ=1,4
179      IBS=IFIX((1.+FO(IJ))*64.)+1
180      PU(IRS)=PU(IRS)+DP(IJ)
181      PI=PI+DP(IJ)
182      PAVG=PAVG+ABS(DP(IJ))/4.
183 C      CALCULATE BINS FOR DELAY
184      IBT = IFIX(1. + 1000.*DEL(IJ)/IDX) + 1
185      IF (IBT .LE. 1) IBT = 1
186      IF (IBT .GE. 100) IBT = 100
187      PDEL(IRT) = PDEL(IRT) + DP(IJ)
188 41 CONTINUE
189 C
190      X=X+DX
191      IF(PAVG.LT.1.E-3*DP1.AND.X.LT.3.*DX) GO TO 32
192 C      ABOVE TERMINATES INTEGRATION
193      IF(PAVG.LT.1.E-3*DP1) GO TO 30
194 C      ABOVE TERMINATES X INTEGRATION AND STEPS TO NEXT Y
195      GO TO 31
196 32 CONTINUE
197      FDO=-SIN(TH*PI/180.)*COS(PHV*PI/180.)
198      FDD = COS(PHV*PI/180.)*(XS-XP)/REF
199 C      DOPPLER SHIFT IN HZ
200      DDO = FDO*F*VEF*10./3.
201      DDD = FDD*F*VEF*10./3.
202      IBS=IFIX((1.+FDD)*64.)+1
203 C
204 C      AIRCRAFT ANTENNA PATTERN IN SATELLITE DIRECTION IS
205 C      ANTP = ANTP(TH,PP)
206 C      PP = 180. - PHV
207 C      RECEIVER POLARIZATION IN SATELLITE DIRECTION IS
208 C      CTH = CTH(TH,PP)
209 C      OPH = OPH(TH,PP)
210 C
211      ANTP=1.0
212 C      DIRECT POWER FROM SATELLITE
213      PDIR=ANTP*CARB(ATH*CTH+RPH*DPH)**2*(RSAT/REF)**2
214 C      THE RECEIVED POWER IN WATTS IS PDIR*POWER*GAIN*APERTURE/DIST
215 C      WHERE PDIR HAS BEEN CALCULATED, DIST=4*PI*RSAT**2 AND THE
216 C      OTHER VARIABLES ARE TRANSMITTER POWER, TRANSMITTER ANTENNA GAIN,
217 C      RECEIVER COLLECTING APERTURE AND RANGE FROM SATELLITE TO SPECULAR POINT
218 C
219 C      CALCULATE THE COHERENT POWER
220      CALL COEF(TH,THI,0.,EP,ATH,RPH,CTH,DPH1

```

```

221      *AL,TH,PH,DELI,RCOEF)
222      EX1 = 2.*((2.*PI*F*ROF*10./3.)*COS(THI*PI/180.))**2
223      IF (EX1 .GT. 60.) EX1 = 60.
224      EX2 = EXP(-EX1)
225      RSPEC = EX2*ANIP*(RSAT*CABS(RCOEF)/RELSP)**2
226      PS = 10.*ALOG10(RSPEC/POIR)
227      PT=10.*ALOG10(PT/POIR)
228      WDOF = VEE*F/10.2
229      WRITE(6,55) PT,PS,POIR
230      WRITE(6,64)OOD,ODO,IHS
231      WRITE(6,56) XXMAX,YYMAX,DX
232      WRITE(6,53)WDOF
233      NN=1
234      YMAX=.05
235      YMIN=0.0
236      DO 45 IL=1,128
237      XX=FLOAT(IL)
238      YY(1)=PO(IL)
239      IND=IL-1
240      CALL PLOT(XX,YY,NN,IND,YMAX,YMIN)
241 45 CONTINUE
242      WRITE(6,61) DELSP
243      WRITE(6,62)IOX
244      NN = 1
245      YMAX = .05
246      YMIN = 0.
247      DO 46 IM = 1,100
248      XX = FLOAT(IM)
249      YY(1) = POEL(IM)
250      IND = IM-1
251      CALL PLOT(XX,YY,NN,IND,YMAX,YMIN)
252 46 CONTINUE
253      CALL EXIT
254      END
255 C
256 C      ***** SUBROUTINES AND FUNCTION SUBPROGRAMS *****
257 C
258 C      SUBROUTINE COEF(THI,THS,PHS,FPS,ATI,BPI,CTS,DPS,AL,TH,PH,DELI,DELS
259 C      *RCOEF)
260 C      COMPLEX ATI,BPI,CTS,DPS,RCOEF,RPAR,RPER,EPS
261 C      GIVEN THE INCIDENCE AND SCATTERING DIRECTIONS,THE POLARIZATION
262 C      STATE OF THE TRANSMITTER AND RECEIVER,AND THE COMPLEX DIELECTRIC
263 C      CONSTANT;THIS SUBROUTINE DETERMINES THE DIRECTION OF THE NORMAL
264 C      TO THE SURFACE REQUIRED FOR SUCH REFLECTION,THE ANGLE ALPHA
265 C      BETWEEN THE NORMAL AND EITHER THE INCIDENT OR REFLECTED
266 C      DIRECTIONS,AND THE COMPLEX REFLECTION COEFFICIENT.
267 C      ALL ANGLES REQUIRED IN DEGREES.
268 C      PI=3.14159265
269 C      THI-THETA ANGLE OF INCIDENCE
270 C      THS-THETA ANGLE OF SCATTER
271 C      PHS- PHI ANGLE OF SCATTER
272 C      ATI-THETA COMPONENT OF THE INCIDENT FIELD
273 C      BPI-PHI COMPONENT OF THE INCIDENT FIELD
274 C      CTS-THETA COMPONENT OF THE SCATTERED FIELD
275 C      DPS- PHI COMPONENT OF THE SCATTERED FIELD

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276 C EPS=COMPLEX DIELECTRIC CONSTANT
277 TH=TH*PI/180.
278 THS=THS*PI/180.
279 PHS=PHS*PI/180.
280 C AL=ANGLE ALPHA BETWEEN INCIDENT DIRECTION AND NORMAL
281 C PH=PHI ANGLE OF THE NORMAL
282 C TH=THETA ANGLE OF THE NORMAL
283 C2AL=-(SIN(THI)*SIN(THS)*COS(PHS)-COS(THI)*COS(THS))
284 CAL=SQRT((1.+C2AL)/2.)
285 AL=ATAN2(SQRT(1.-(CAL)**2),CAL)
286 TH(AL,1.E-3) GO TO 100
287 PH=ATAN2(SIN(THS)*SIN(PHS),SIN(THS)*COS(PHS)-SIN(THI))
288 CTH=(COS(THS)+COS(THI))/(2.*CAL)
289 TH=ATAN2(SQRT(1.-CTH**2),CTH)
290 C DELI=ANGLE DELTA INCIDENCE
291 C DELS=ANGLE DELTA SCATTERED
292 S2AL=SIN(2.*AL)
293 COELI=(SIN(THS)*COS(PHS)*COS(THI)+SIN(THI)*COS(THS))/S2AL
294 SOELI=SIN(THS)*SIN(PHS)/S2AL
295 DELI=ATAN2(SOELI,COELI)
296 COELS=(SIN(THI)*COS(THS)*COS(PHS)+COS(THI)*SIN(THS))/S2AL
297 SOELS=SIN(THI)*SIN(PHS)/S2AL
298 DELS=ATAN2(SOELS,COELS)
299 GO TO 90
300 100 CONTINUE
301 AL=0.0
302 TH=THI
303 PH=PI
304 DELI=0.0
305 DELS=0.0
306 COELI=1
307 SOELI=0.0
308 COELS=1.0
309 SOELS=0.0
310 90 CONTINUE
311 C RPAR=FRESNEL REFLECTION COEFFICIENT FOR PARALLEL POLARIZATION
312 C RPER=FRESNEL REFLECTION COEFFICIENT FOR PERPENDICULAR POLARIZATION
313 C RCOEF=COMPLEX REFLECTION COEFFICIENT
314 RPAR=(EPS*COS(AL)-CSQRT(EPS-SIN(AL)**2))/(EPS*COS(AL)+CSQRT(EPS-SI
315 *N(AL)**2))
316 RPER=(COS(AL)-CSQRT(EPS-SIN(AL)**2))/(COS(AL)+CSQRT(EPS-SIN(AL)**2
317 *))
318 RCOEF=-RPER*((RPI*COELI-ATI*SDELI)*(DPS*COELS+CTS*SDELS))+RPAR*((A
319 *TI*COELI+PI*SDELI)*(CTS*COELS-DPS*SDELS))
320 AL=AL*180./PI
321 TH=TH*180./PI
322 PH=PH*180./PI
323 THI=THI*180./PI
324 THS=THS*180./PI
325 PHS=PHS*180./PI
326 DELI=DELI*180./PI
327 DELS=DELS*180./PI
328 RETURN
329 END
330 FUNCTION PDEN(TH,PH,S2)

```



```

331 C THIS FUNCTION CALCULATES THE VALUE OF THE PROBABILITY DENSITY
332 C FUNCTION (PDEN) FOR A SURFACE NORMAL WHERE TH IS THE THETA-ANGLE
333 C IN DEGREES AND PH IS THE PHI-ANGLE IN DEGREES OF THE SURFACE NORMAL
334 C AND S2 IS THE MEAN SQUARE SLOPE. THE PDF IS GAUSSIAN.
335 P1=3.14159265
336 TH=TH*PI/180.
337 A=-TAN(TH)*TAN(TH)/(S2*(1.+2.*S2))
338 IF(ABS(A).GT.60.) A=-60.
339 PDEN=COS(TH)*EXP(A)/(PI*S2)
340 TH=TH*180./PI
341 RETURN
342 END
343 COMPLEX FUNCTION EPS(F,T,S)
344 C COMPLEX DIELECTRIC OF SEA WATER EPS (STOGRYN MTT)
345 C T IN CENTIGRADE, F IN GIGAHERTZ, S IS SALINITY IN P.P.THOU.
346 REAL N
347 C NORMAL SEA WATER RANGES FROM 20. TO 35. PPT
348 N = S*(.01707 + .00001205*S + S*S*4.058E-9)
349 C = 25. - T
350 AA = 1.649E-5 - C*(1. - .1*C)*2.551E-7
351 D = EXP(C*(.02033+.0001268*C+C*C*2.464E-6-S*AA))
352 SIG = S*(.162521-.0014619*S+.00002093*S*S -S*S*S*1.282E-7)/D
353 DD = .11109 - .003824*T + .0000694*T*T
354 W = (1. + .001463*N*T - .049*N - .02967*N*N)*DD
355 EO = (1.-.2551*N+.0515*N*N)*(87.74-.4008*T+.00094*T*T)
356 EPS = 4.9 + (EO-4.9)/CMPLX(1. , W*F) - CMPLX(0.,17.95*SIG/F)
357 RETURN
358 END
359 SUBROUTINE PLOT( X,Y,N,IND,YMAX,YMIN)
360 DIMENSION M(119),YLABEL(6),Y(10),MARK(10)
361 DATA MARK(1),MARK(2),MARK(3),MARK(4),MARK(5),MARK(6),MARK(7),MARK(8),
362 MARK(9),MARK(10),MARK(4)/1H*,1H.,1H1,1H0,1HN,1HH,1H1,1H2,1H-,1HX/
363 DATA IPLANK,NOPT,IPLUS/1H .1HS,1H+/
364 IF(IND)1,1,11
365 1 WRITE(6,3)
366 3 FORMAT(//25X,'ORDER IN WHICH PLOT SYMBOLS ARE USED *.IXONH1Z-',
367 *//30X,'THE SYMBOL ($) INDICATES OFF-SCALE DATA',//)
368 DO7J=9,119
369 7 M(J)=MARK(10)
370 NCOUNT=10
371 SCALE=100.0/(YMAX-YMIN)
372 LLL=(-YMIN*SCALE)+11.5
373 DO8J=1,6
374 8 YLABEL(J)=M*20.0/SCALE+YMIN
375 WRITE(4,9) (YLABEL(I),I=1,6)
376 9 FORMAT(6X,1PE9.2,5(1PE20.2) / )
377 GOTO132
378 11 NCOUNT=NCOUNT+1
379 DO99J=1,119
380 99 M(J)=IPLANK
381 IF(LLL.GE.11.AND.LLL.LE.110)M(LLL)=MARK(10)
382 IF(NCOUNT-10)133,132,133
383 132 DO89J=11,111,20
384 89 M(J)=IPLUS
385

```

```

386 13X GO20J=1,0
387     L=(Y(J)-YFIN)*SCALF+0.5
388     IF(L)14,17,17
389 14 IF(L+1)15,16,16
390 15 M(1)=MUP1
391     GO2020
392 16     LL=L+11
393     M(LL)=MARK(J)
394     GO2020
395 17 IF(L-108)18,19,19
396 18     LL=L+11
397     M(LL)=MARK(J)
398     GO2020
399 19 M(119)=MUP1
400 20 CONTINUE
401     IF(NCOUNT-10)21,25,21
402 21 WRITE(6,24) (M(J), J=1,119)
403 24 FORMAT(1X,119A1)
404     GO2027
405 25 WRITE(6,26) (X,(M(J),J=9,119))
406 26 FORMAT(1X,F8.3 ,111A1)
407     NCOUNT=0
408 27 CONTINUE
409     RETURN
410     ENDS

```

APPENDIX II SAMPLE OUTPUT (Curve B Fig. 8)

TEM(C)=10.000 SAL(PPT)=35.000 F(GHZ)= 1.400 SEA SLOPE(DEG)=15.00 SEA HEIGHT= .30M
 THETA INC= 45.0000 PHI(PLANE VEL)= 90.0000 PLANE HEIGHT(M)= .300000E 4 VELOCITY=200.0000M/S
 RTH= .7070 0.0000 RPH= 0.0000 .7070 CTH= 1.0000 0.0000 DPH= 0.0000 0.0000

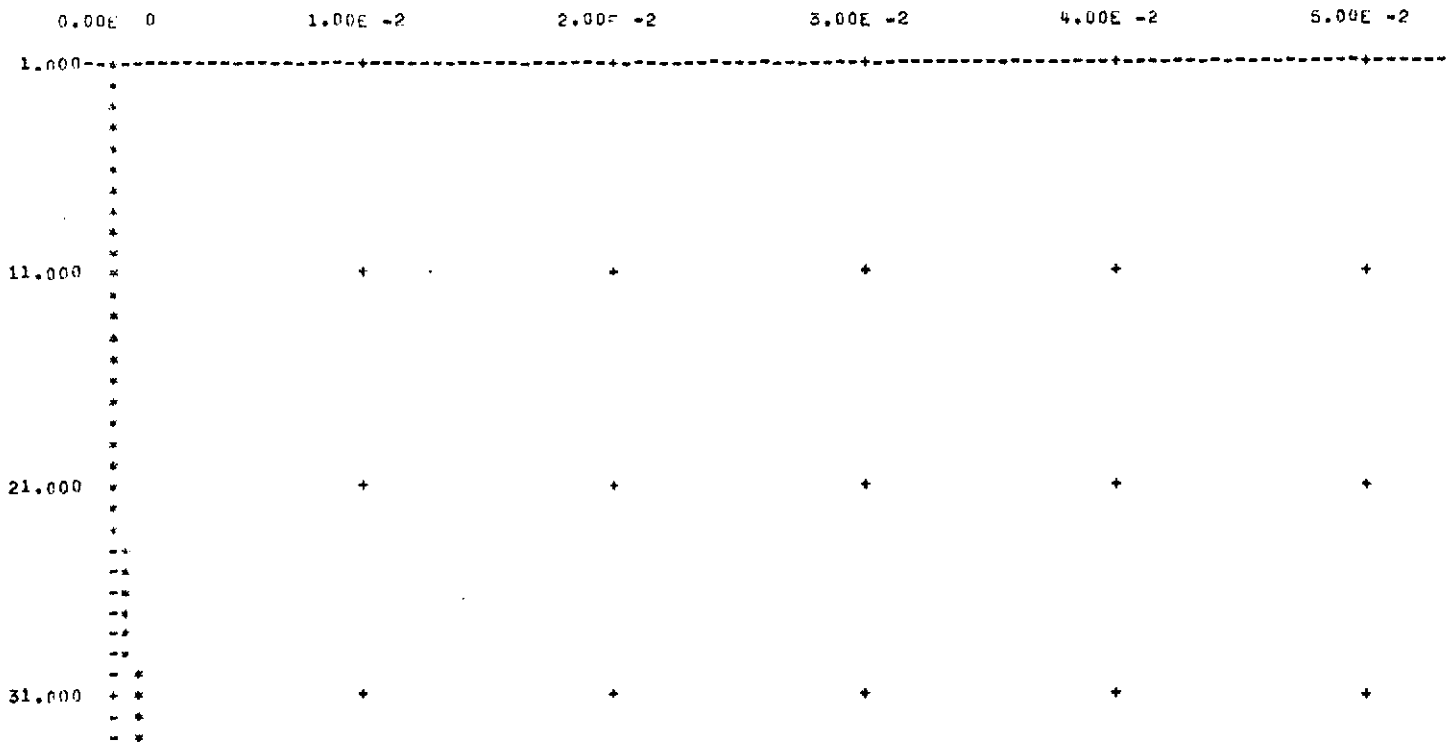
FINITE RANGE CASE JJJ IS 30
 EPS= 71.57 -56.03 J

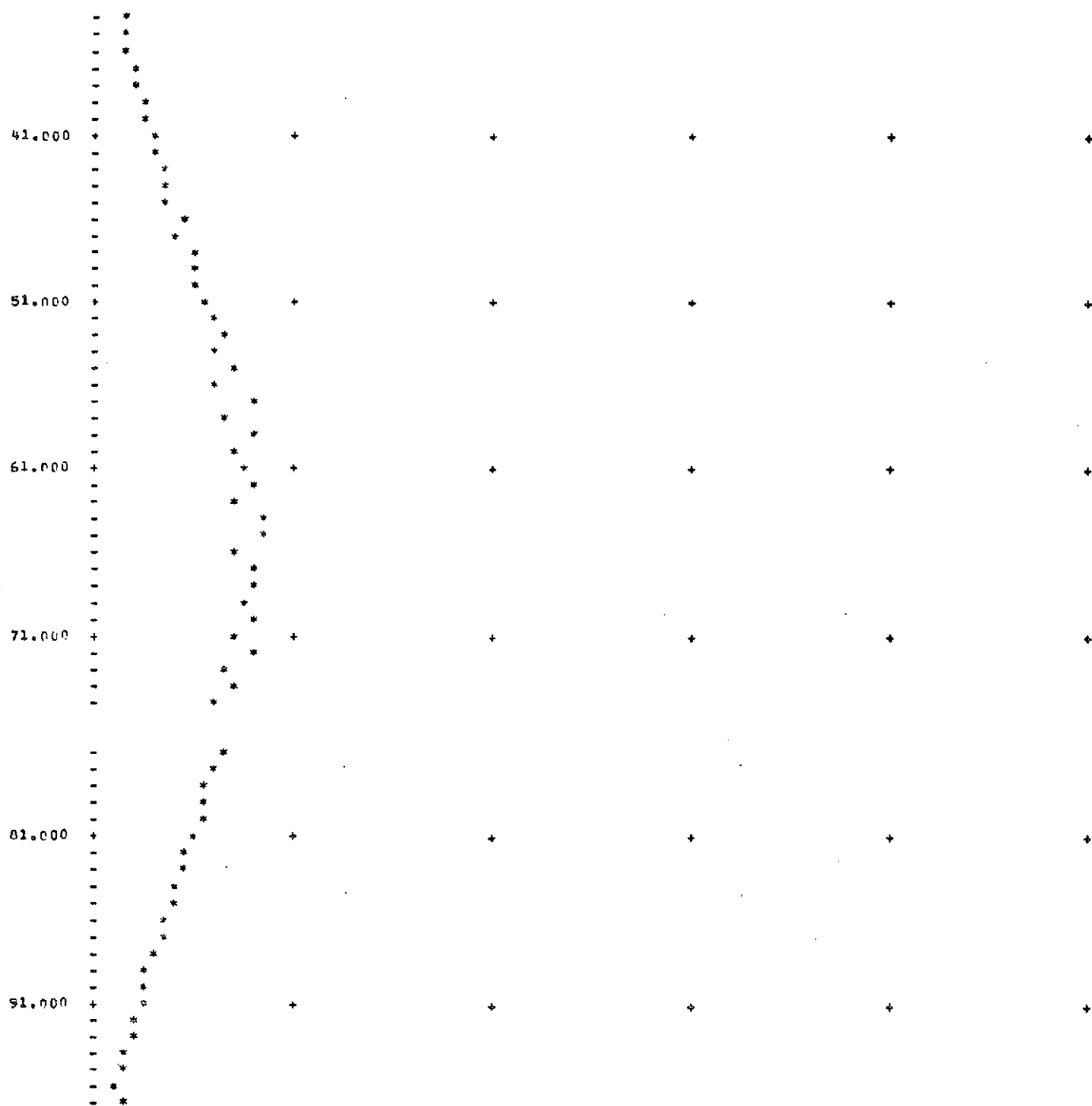
DIFFUSE POWER IS -1.894308; COHERENT POWER IS -262.3041 DB BELOW DIRECT POWER OF .49985
 DIRECT DOPPLER IS -.000 HZ; SPECULAR DOPPLER IS -.000 HZ IN BIN 64
 MAX VALUES OF X AND Y IN INTEGRATION YMAX= .310285E 5 YMAX= .519821E 4 DELTX = .1072E 3

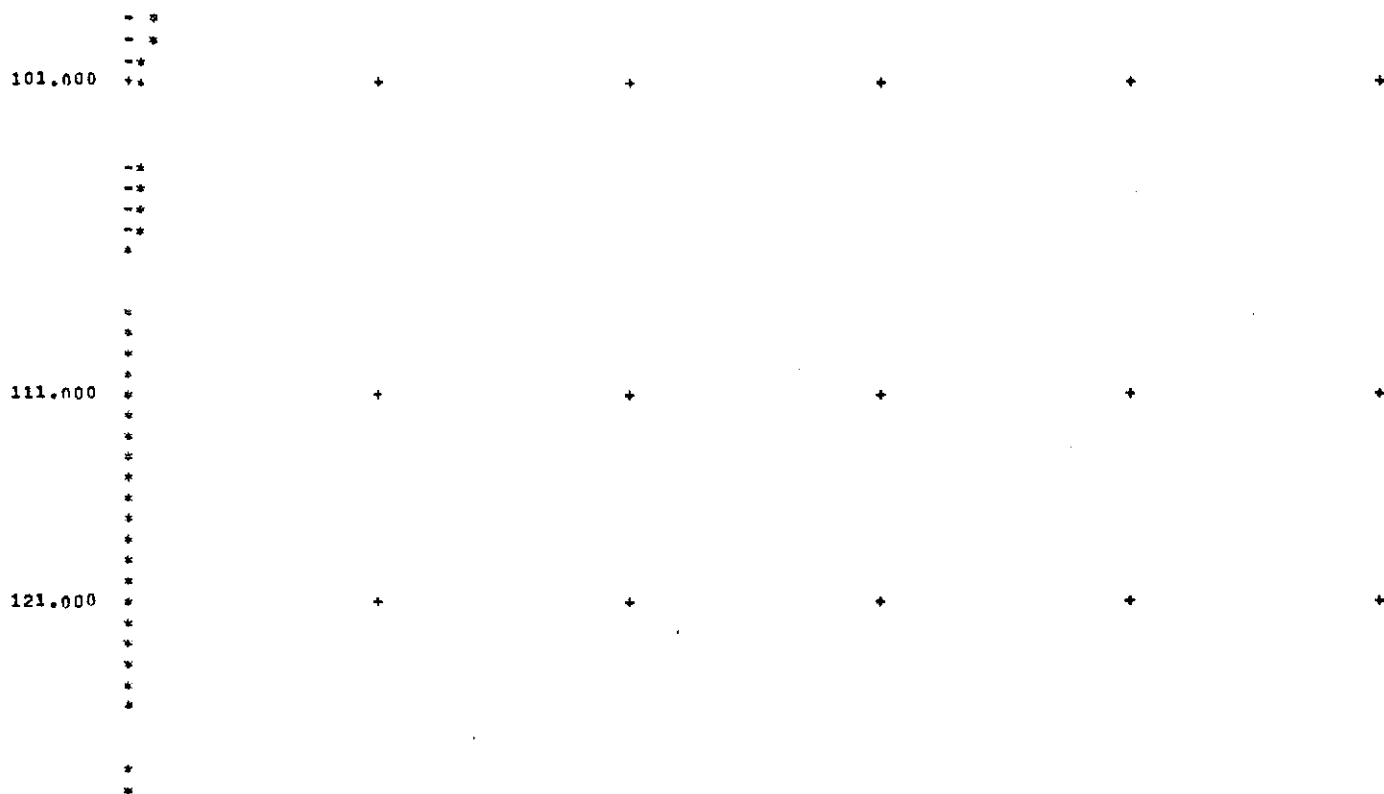
GRAPH OF POWER SPECTRUM BIN WIDTH IS 14.5833HZ

ORDER IN WHICH PLOT SYMBOLS ARE USED *.IXONHIZ=

THE SYMBOL (\$) INDICATES OFF-SCALE DATA





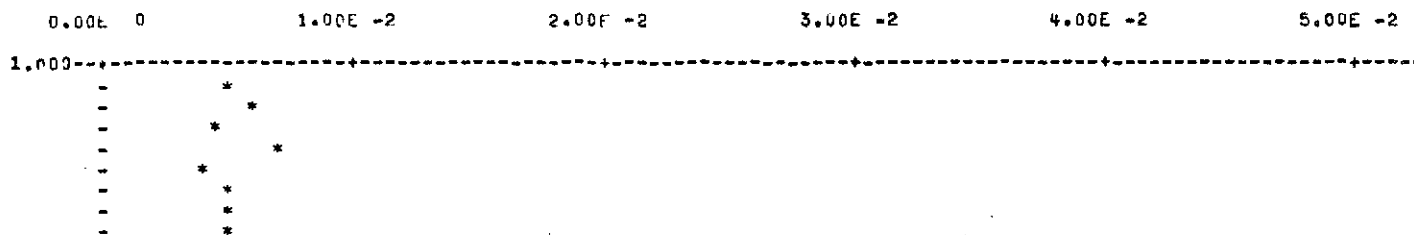


POWER VS DELAY; SPECULAR DELAY IS 14.1413MICROSEC

SPEC POINT IN BIN 2; BIN WIDTH IS 2 NANOSEC

ORDER IN WHICH PLOT SYMBOLS ARE USED *.IXONH1Z-

THE SYMBOL (\$) INDICATES OFF-SCALE DATA



11.000	-	*						
	+		*	+		+		+
	-		*					
	-							
	-		*					
	-		*					
	-		*					
	-		*					
	-		*					
21.000	+	*		+		+		+
	-	*						
	-	*						
	-	*						
	-	*						
	-	*						
	-	*						
	-	*						
	-	*						
	-	*						
31.000	+	*		+		+		+
	-	*						
	-	*						
	-	*						
	-	*						
	-	*						
	-	*						
	-	*						
	-	*						
	-	*						
41.000	+	*		+		+		+
	-	*						
	-	*						
	-	*						
	-	*						
	-	*						
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	-	*						
	-	*						
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51.000	+	*		+		+		+
	-	*						
	-	*						
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61.000	+	*		+		+		+
	-	*						
	-	*						
	-	*						
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	-	*						
	-	*						
	-	*						
	-	*						
71.000	+	*		+		+		+
	-	*						
	-	*						

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